# Inverse function of mortality as a measure of longevity extension

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### Motivation

Three approaches to the operational definition of 'old' ages:

- ages associated with a person's later stage of life, starting 65 or 70
- 2. ages corresponding to the old-age death heap in the age distribution of deaths
- 3. ages at high levels of adult mortality

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Three potential indicators:

- 1. life expectancy at some selected old ages such as  $e_x$
- 2. the late modal age at death,  ${\cal M}$
- 3. age-of-mortality indicator, AoM

- 1. Investigate the use of *AoM* as possible measures of longevity extension
- 2. Conduct a methodological investigation by comparing AoM with  $e_x \mbox{ and } M$

### Data & Methods

Human Mortality Database (HMD)

- data series: death counts and population exposure's by single year of age, calendar year, and sex
- countries: The Group of Seven (G7), i.e. Canada, France, Germany, Italy, Japan, UK, and US
- period: 1970-most recent available year

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For each country, calendar year, and sex:

• 
$$e_{65} = \int_{65}^{\omega} exp \left[ -\int_{65}^{\omega} \mu(u) du \right]$$

- $M = \max_x f(x) = \max_x \mu(x) exp \left[ -\int_{10}^{\omega} \mu(u) du \right]$
- the AoM indicator derived from the age-of-mortality function,  $\nu(y)$   $\nu(y)=\mu^{-1}(y)$

 $\mu(x)$  was estimated using Poisson *P*-splines smoothing.

Force of mortality,  $\mu(x),$  and the inverse of the force of mortality,  $\mu^{-1}(y),$  resulting from nonparametric P-splines smoothing



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## International trends and differentials in AoMs, females, G7 countries



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## Trends and differentials in $\nu(0.1)$ , $e_{65}$ , and M, females, G7 countries



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•  $65 + e_{65,1970} = 82.5$   $65 + e_{65,2016} = 87.2$  $\Delta e_{65} = 4.7$ 

• 
$$\nu(0.1)_{1970} = 84.4$$
  
 $\nu(0.1)_{2016} = 89.5$   
 $\Delta\nu(0.1) = 5.1$ 

• 
$$M_{1970} = 84.5$$
  
 $M_{2016} = 91.3$   
 $\Delta M = 6.8$ 

#### Old-age compression of mortality, females, Canada



### Trends in AoM at mortality level of total life expectancy at age 65 and of modal age at death in 1970, females, Canada



- $65 + e_{65,1970} = 82.5$   $65 + e_{65,2016} = 87.2$  $\Delta e_{65} = 4.7$
- $\nu(\mu(65 + e_{65,1970}))_{1970} = 82.5$   $\nu(\mu(65 + e_{65,1970}))_{2016} = 88.0$  $\Delta\nu(\mu(65 + e_{65,1970})) = 5.5$
- $M_{1970} = 84.5$  $M_{2016} = 91.3$  $\Delta M = 6.8$
- $\nu(\mu(M_{1970}))_{1970} = 84.5$   $\nu(\mu(M_{1970}))_{2016} = 89.6$  $\Delta\nu(\mu(M_{1970})) = 5.1$

### Trends in AoM at mortality level of total life expectancy at age 65 and of modal age at death in 1970, females, G7 countries



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Our study showed:

- the *AoM* indicator at the three selected levels of old-age mortality increased since 1970 in G7 countries,
- the shift in AoM to older ages occurred at faster pace at lower than higher mortality levels,
- $\nu(0.1)$  increased more rapidly than  $e_{65}$  and more slowly than M since 1970 in all G7 countries,
- use of AoM indicators in complementarity to  $e_x$  and M.

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Towards:

- an analysis and comparison of the pace of increase in  $e_{65},$   $\nu(0.1),$  and M,
- construction of a composite AoM indicator.

#### Thank you for your attention

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